

Physics

1. ©

$$B = \frac{\mu_0}{4\pi} \cdot \frac{2i}{r} \Rightarrow B \propto \frac{1}{r}$$

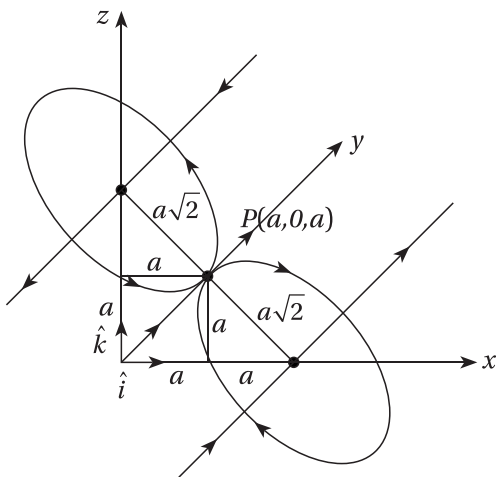
B - r curve is a rectangular hyperbola.

2. Ⓐ

3. Ⓑ

$$\begin{aligned} B &= B_1 (\odot) - B_2 (\otimes) \\ &= \frac{1}{2} \left(\frac{\mu_0 I}{2R_1} - \frac{\mu_0 I}{2R_2} \right) (\odot) \\ &= \frac{1}{2} \left[\frac{\mu_0 I}{2} \left(\frac{1}{R_1} - \frac{1}{R_2} \right) \right] (\odot) \\ \Rightarrow B &= \frac{\mu_0 I (R_2 - R_1)}{4R_1 R_2} \end{aligned}$$

4. Ⓓ



$$\hat{u} = \frac{\hat{i} + \hat{k}}{\sqrt{1^2 + 1^2}} = \frac{1}{\sqrt{2}} (\hat{i} + \hat{k})$$

[2]

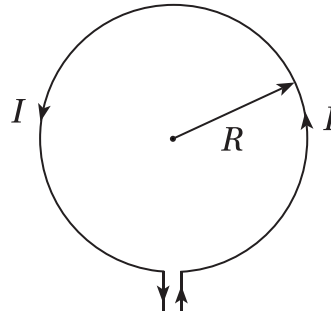
5. (A)

6. (B)

$$M = I\pi R^2$$

$$2\pi R = L \Rightarrow R = \frac{L}{2\pi}$$

$$M = I\pi \cdot \frac{L^2}{4\pi^2} = \frac{IL^2}{4\pi} \odot$$



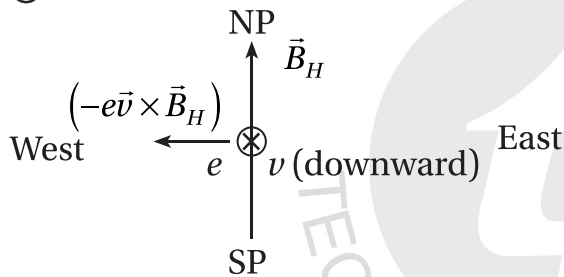
7. (C)

$$F = qvB \sin \theta$$

$$F = F_{\max} \text{ for } \sin \theta = 1 \Rightarrow \theta = \frac{\pi}{2}$$

$$F_{\max} = qvB$$

8. (A)



9. (C)

$$r = \frac{mv}{qB} \Rightarrow p = qBr \text{ (magnitude constant)}$$

But v changes its direction in circular path.

10. (D)

$$\Phi = 6t^2 - 5t + 1$$

$$R = 10 \Omega$$

$$\frac{d\Phi}{dt} = 12t - 5$$

$$t = 0.25 \text{ s}$$

$$\Rightarrow \varepsilon = -\frac{d\Phi}{dt} = 5 - 12t$$

$$\Rightarrow t = \frac{1}{4} \text{ s}$$

$$\Rightarrow i = \frac{\varepsilon}{R} = \frac{5 - 12t}{10} = \frac{1}{2} - \frac{6}{5}t$$

$$\Rightarrow i = \frac{1}{2} - \frac{6}{5} \cdot \frac{1}{4} = \frac{1}{2} - \frac{3}{10}$$

$$\Rightarrow i = \frac{5 - 3}{10} = \frac{2}{10} = 0.2 \text{ A}$$

[3]

11. (B)

12. (A)

13. (B)

$$i = 5 + 10 \sin \omega t \quad a = 5$$

$$I_{\text{eff}} = \sqrt{a^2 + \frac{b^2}{2}} = \sqrt{25 + \frac{100}{2}} = \sqrt{25 + 50} = \sqrt{75} = \sqrt{3 \times 25}$$

$$I_{\text{eff}} = 5\sqrt{3}$$

14. (B)

$$X_L = 100 \Omega$$

$$f = 50 \text{ Hz} \quad X_L = \omega L$$

$$\omega = 2\pi f = 100\pi$$

$$100 \text{ pL} = 100$$

$$\Rightarrow L = \frac{1}{\pi} = 0.32 \text{ H}$$

15. (A)

$$I = \frac{E}{\sqrt{R^2 + \omega^2 L^2}}$$

If E is steady emf as it comes from Battery we get ($L = 0$)

$$I = \frac{E}{R}$$

16. (A)

17. (B)

18. (C)

19. (C)

20. (B)

21. (B)

22. (A)



23. (A)

$$qvB = qE \Rightarrow vB = E = \frac{V}{d}$$

$$\Rightarrow V = vBd = 3.8 \times 10^6 \times 0.2 \times 1.5 \times 10^{-2}$$

$$\Rightarrow V = 1.14 \times 10^4 \text{ Volts}$$

(downward field)

24. (D)

α -particle gets deflected downward i.e., path III.

β -particle (electron) gets deflected upward.

25. (C)

$$v_1 = 4.4 \times 10^6 \text{ ms}^{-1}$$

$$v_2 = 3.8 \times 10^6 \text{ ms}^{-1}$$

$$x = v_1 t$$

$$y = \frac{1}{2} \cdot \frac{2e}{4m_H} \cdot \frac{V}{d} t^2$$

$$\Rightarrow y = \frac{e}{4m_H} \cdot \frac{V}{d} t^2$$

$$\Rightarrow y = \frac{e}{4m_H} \cdot \frac{vBd}{d} \cdot t^2$$

$$\Rightarrow y = \frac{e}{4m_H} \cdot vB \cdot t^2$$

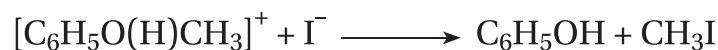
$$y = \frac{1.6 \times 10^{-19}}{4 \times 1.6 \times 10^{-27}} \times 4.4 \times 10^6 \times 0.2 t^2$$

$$= 1.1 \times 0.2 \times 10^{14} t^2 = 1.12 \times 10^{14} t^2$$

Chemistry

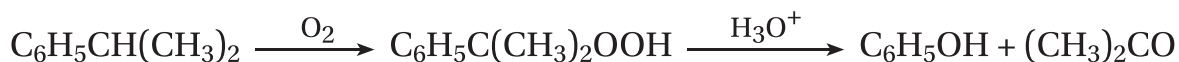
26. (B)

Related equations are



As, $\text{C}_6\text{H}_5\text{OH}$ is an aromatic compound hence attack by the nucleophile (I^-) is too much difficult.

27. Ⓓ



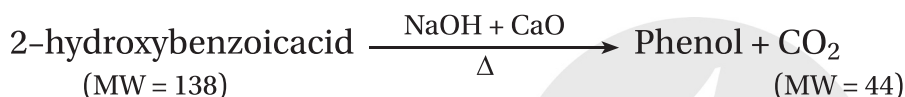
So, the biproduct is $(\text{CH}_3)_2\text{CO}$. It contains ketomethyl ($\text{CH}_3\text{CO}-$) group hence it takes part in haloform reaction. It takes part in aldol condensation reaction but does not take part in Cannizaro's reaction.

Its tautomer is $\text{H}_2\text{C} = \text{C}(\text{OH})\text{CH}_3$ and its functional isomer is $\text{CH}_3\text{CH}_2\text{CHO}$.

28. Ⓐ

4-nitrophenol is the strongest Bronsted acid as its conjugate base is the most stable due to resonance. Now, resonance contribution of 2-nitrophenate ion is lower than 4-nitrophenate ion.

29. Ⓒ

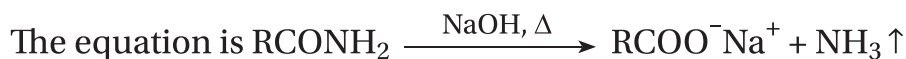


So, 1.1 gm CO_2 is formed by $\frac{138 \times 1.1}{44} = 3.45$ gm 2-hydroxybenzoic acid

Now, 1 mole acid can react with 1 mole ethanoyl anhydride to form aspirin.

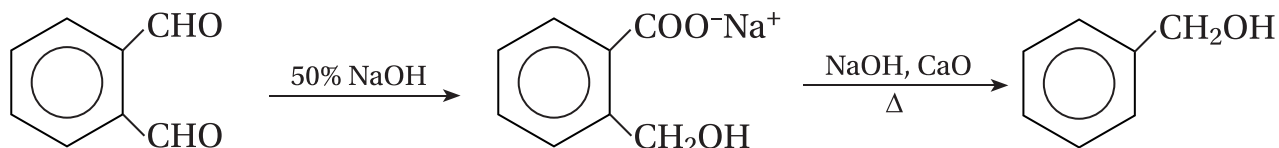
Now, 3.45 gm 2-hydroxybenzoic acid reacts with $\frac{102 \times 3.45}{138} = 2.55$ gm ethanoyl anhydride

30. Ⓑ

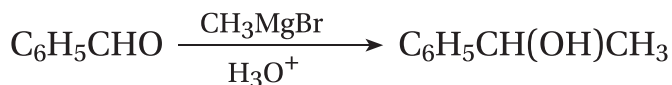


So, only amide group takes part in this reaction.

31. Ⓑ

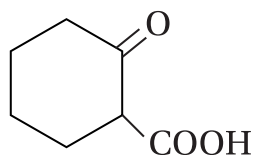
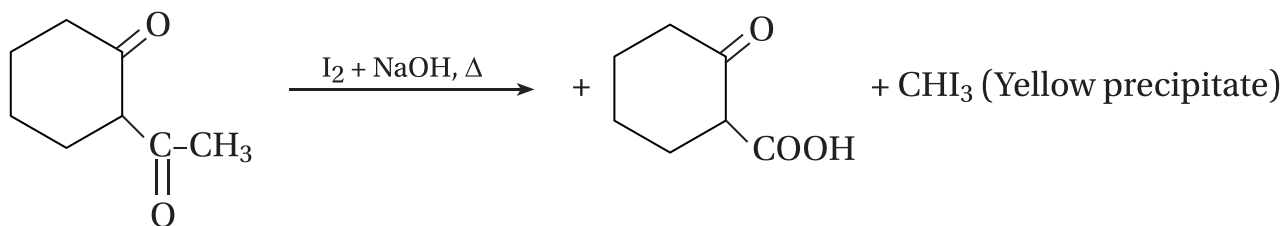


$-\text{CH}_2\text{OH}$ is ortho / para orienting group. Benzyl alcohol is weaker Bronsted acid than phenol. As benzyl alcohol is a primary alcohol so, it does not take part in Lucas test spontaneously.

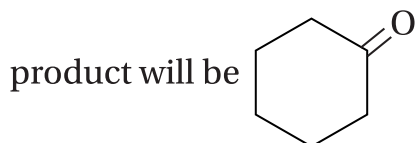


[6]

32. Ⓑ



is a β -ketoacid. Hence on heating it releases CO_2 gas. So, the final



33. Ⓐ

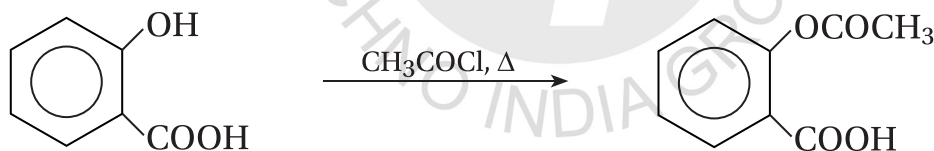
$CH_3C \equiv CCOOH$ the s-character of α -carbon is 50%. So, it is the strongest Bronsted acid

$CH_3CH = CHCOOH$ the s-character of α -carbon is 33.33%.

$CH_3CH_2CH_2COOH$ the s-character of α -carbon is 25%.

Alcohol is weaker Bronsted acid than carboxylic acid.

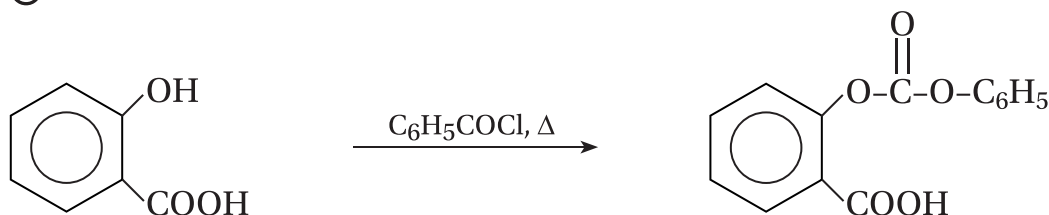
34. Ⓓ



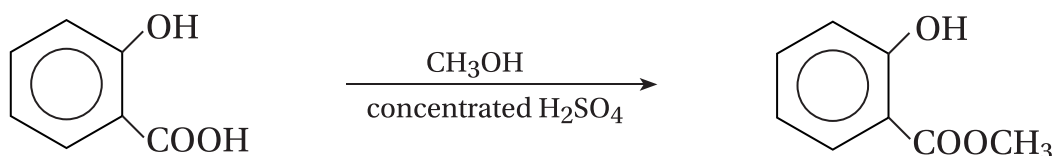
35. Ⓓ

2-hydroxybenzoic acid is produced by using Kolbe - Schmidt reaction

36. Ⓓ



37. Ⓒ



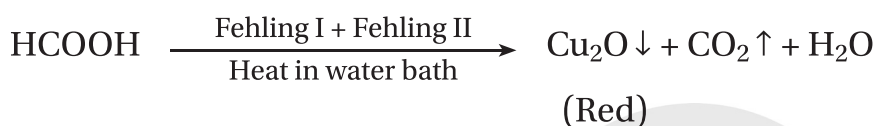
38. (A)



39. (B)

C-Cl bond is weaker than C-C bond and C-O bond. Hence, chloride is released from the molecule very easily

40. (B)



41. (C)



As the solutions are isotonic,

$$i_{(\text{Na}_2\text{SO}_4)} C_{(\text{Na}_2\text{SO}_4)} = C_{(\text{C}_6\text{H}_{12}\text{O}_6)}$$

$$\therefore i_{\text{Na}_2\text{SO}_4} = \frac{0.01}{0.004} = 2.5$$

$$\alpha = \frac{(i-1)}{n-1} = \frac{(2.5-1)}{3-1} = 0.75$$

So, degree of dissociation = 75%

42. (A)

$$t_{50\%} \propto \frac{1}{(\text{initial concentration})^{\text{order}-1}}$$

So, it is a third order reaction and all the given equations are true for third order reactions

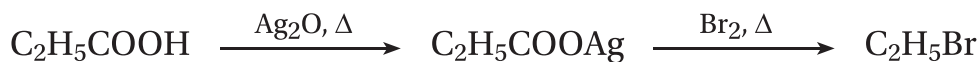
43. (B)

The voltage of the cell depends on the concentration of the electrolytes not on the dimension of electrodes.

44. Ⓑ

Correct order of reducing power is $D > A > H_2 > B$. So, metal B cannot react with dilute H_2SO_4 solution.

45. Ⓓ

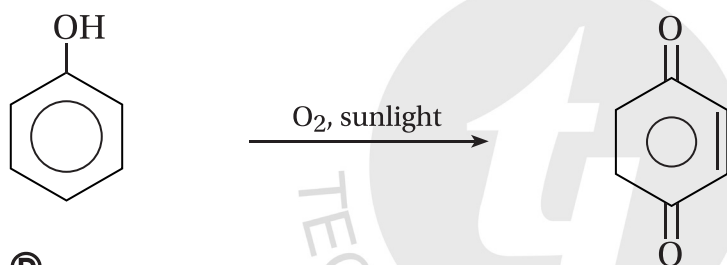


C_2H_5Br contains primary carbon only.

46. Ⓓ

The alkyl group are the hydrophobic part in an alcohol molecule. Now, larger the size of alkyl group, higher is the extent of repulsion with water. So, solubility decreases.

47. Ⓐ



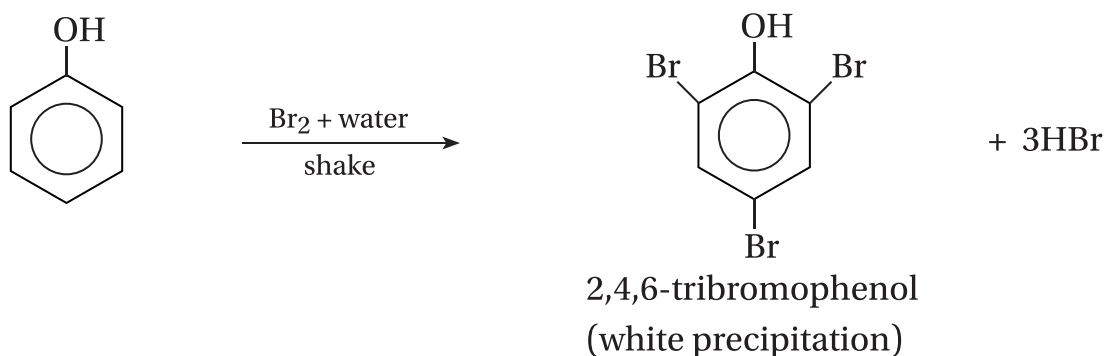
48. Ⓓ

If the alkyl group in the carboxylic acid contains strongly electron withdrawing group then the conjugate base becomes more stable and hence the acid becomes strong.

49. Ⓐ

Lone pair in amide group takes part in resonance and hence lone pair donation power decreases. But this resonance is not possible in case of $CH_3CH_2CH_2NH_2$.

50. Ⓒ



51. (A)

$$\int \frac{\sqrt{\tan x}}{\sin x \cos x} dx = \int \frac{\sqrt{\tan x}}{\tan x} \times \sec^2 x dx = \int \frac{\sec^2 x}{\sqrt{\tan x}} dx = 2\sqrt{\tan x} + c$$

52. (C)

$$\text{Let, } a^2 \cos^2 x + b^2 \sin^2 x = t$$

$$\Rightarrow (-2a^2 \cos x \sin x + 2b^2 \sin x \cos x) dx = dt$$

$$\Rightarrow (b^2 - a^2) \sin 2x dx = dt$$

$$\Rightarrow \sin 2x dx = \frac{dt}{b^2 - a^2}$$

$$\Rightarrow \int \frac{\sin 2x dx}{a^2 \cos^2 x + b^2 \sin^2 x} = \frac{1}{b^2 - a^2} \int \frac{dt}{t} = \frac{1}{b^2 - a^2} \log t + c = \frac{1}{b^2 - a^2} \log |a^2 \cos^2 x + b^2 \sin^2 x| + c$$

53. (C)

$$\int \frac{dx}{x(x^4 - 1)} = \int \frac{x dx}{x^2(x^4 - 1)} = \frac{1}{2} \int \frac{dt}{t(t^2 - 1)}$$

$$= \frac{1}{2} \int \frac{dt}{t(t+1)(t-1)} = \frac{1}{4} \left[\int \frac{1}{t-1} dt - \int \frac{2}{t} dt + \int \frac{1}{t+1} dt \right]$$

$$= \frac{1}{4} [\log(t-1) - 2\log t + \log(t+1)] + c = \frac{1}{4} \log \left(\frac{t^2 - 1}{t^2} \right) + c = \frac{1}{4} \log \left(\frac{x^4 - 1}{x^4} \right) + c$$

54. (A)

$$\int \frac{dx}{(2+x)\sqrt{1+x}} = \int \frac{dx}{(1+1+x)\sqrt{1+x}} \quad \text{Let } 1+x = t^2 \Rightarrow dx = 2t dt$$

$$= \int \frac{2t dt}{(1+t^2)t} = 2 \int \frac{dt}{1+t^2} = 2 \tan^{-1}(t) + c = 2 \tan^{-1}(\sqrt{1+x}) + c$$

55. (A)

$$I = \int_0^\pi \frac{x \sin x dx}{2 - \sin^2 x} = \int_0^\pi \frac{(\pi - x) \sin(\pi - x)}{2 - \sin^2(\pi - x)} dx$$

$$2I = \pi \int_0^\pi \frac{\sin x dx}{2 - \sin^2 x} = \pi \int_0^\pi \frac{\sin x dx}{1 + \cos^2 x}$$

[10]

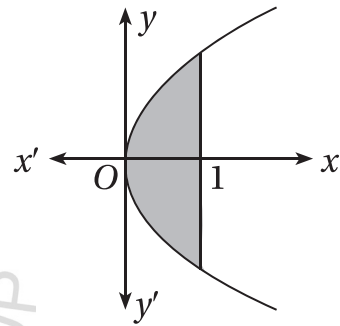
$$\begin{aligned} \Rightarrow I &= -\frac{\pi}{2} \int_0^{\pi} \frac{d(\cos x)}{1 + \cos^2 x} = -\frac{\pi}{2} \left[\tan^{-1}(\cos x) \right]_0^{\pi} \\ &= -\frac{\pi}{2} \left[-\frac{\pi}{4} - \frac{\pi}{4} \right] = \frac{\pi^2}{4} \end{aligned}$$

56. (A)

$$\begin{aligned} \int_0^{\pi} \sqrt{\frac{1 + \cos 2x}{2}} dx &= \int_0^{\pi} \sqrt{\cos^2 x} dx = \int_0^{\pi} |\cos x| dx = \int_0^{\pi/2} \cos x dx + \int_{\pi/2}^{\pi} -\cos x dx \\ &= [\sin x]_0^{\pi/2} - [\sin x]_{\pi/2}^{\pi} = 1 + 1 = 2 \end{aligned}$$

57. (B)

$$\begin{aligned} \text{Area} &= 2 \int_0^1 2\sqrt{x} dx = 4 \left[\frac{2}{3} x^{3/2} \right]_0^1 \\ &= \frac{8}{3} [1 - 0] \text{ sq. unit} = \frac{8}{3} \text{ sq. unit} \end{aligned}$$



58. (A)

$$\int_{-2}^2 \log\left(\frac{1+x}{1-x}\right) dx = 0$$

because $f(x) = \log\left(\frac{1+x}{1-x}\right)$ is odd function.

\therefore (A) is true.

(R) : If $f(x)$ is an odd function, then

$$\int_{-a}^a f(x) dx = 0 \quad \text{True}$$

(R) is the correct explanation of (A).

59. (A)

$$(A) : \int [\sin(\log x) + \cos(\log x)] dx = \int d[x \sin(\log x)] = x \sin(\log x) + c \quad \text{True}$$

$$(R) : \frac{d}{dx} [x \sin(\log x)] = \sin(\log x) + \cos(\log x) \quad \text{True}$$

(R) is the correct explanation of (A).

60. (B)

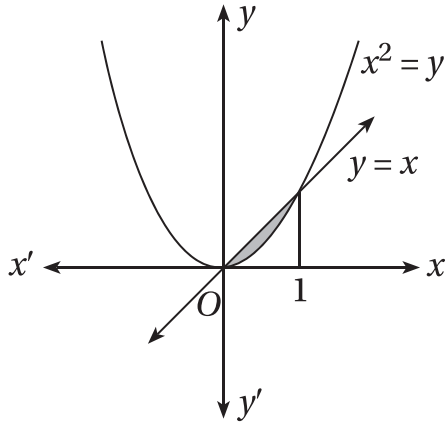
$$x^2 = y, y = x$$

$$\Rightarrow x^2 = x \Rightarrow x^2 - x = 0 \Rightarrow x(x-1) = 0 \quad \therefore x = 0, x = 1$$

when $x = 0, y = 0 \quad \therefore$ point is $(0, 0)$

when $x = 1, y = 1 \quad \therefore$ point is $(1, 1)$

61. (A)



62. (A)

$$\text{Area} = \int_0^1 (x - x^2) dx = \left[\frac{x^2}{2} - \frac{x^3}{3} \right]_0^1 \text{ sq.unit} = \left(\frac{1}{2} - \frac{1}{3} \right) \text{ sq.unit} = \frac{1}{6} \text{ sq.unit}$$

63. (B)

$$\int \sqrt{1+x^2} d(x^2) = \int \sqrt{1+x^2} d(1+x^2) = \frac{2}{3} (1+x^2)^{3/2} + c$$

64. (A)

$$I = \int_0^{\pi/2} \log(\tan x) dx = \int_0^{\pi/2} \log \left\{ \tan \left(\frac{\pi}{2} - x \right) \right\} dx = \int_0^{\pi/2} \log \cot x dx$$

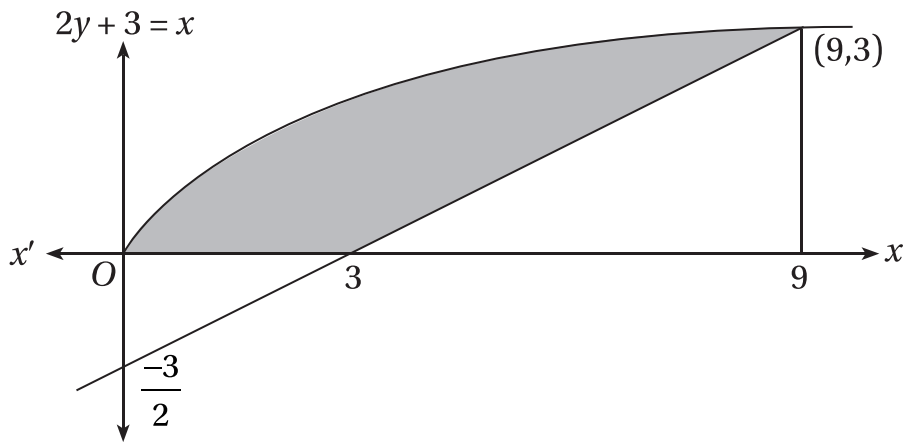
$$\therefore 2I = \int_0^{\pi/2} [\log(\tan x) + \log(\cot x)] dx$$

$$\Rightarrow 2I = \int_0^{\pi/2} \log(\tan x \cot x) dx = 0$$

$$\therefore I = 0$$

65. (A)

$$y = \sqrt{x} \Rightarrow y^2 = x$$



$$\begin{aligned} \text{Area} &= \int_0^9 \sqrt{x} \, dx - \int_3^9 \left(\frac{x-3}{2} \right) dx = \frac{2}{3} \left[x^{3/2} \right]_0^9 - \frac{1}{2} \left[\frac{x^2}{2} - 3x \right]_3^9 \\ &= \frac{2}{3} \times 27 - \frac{1}{2} \left[\left(\frac{81}{2} - 27 \right) \right] - \left(\frac{9}{2} - 9 \right) = 18 - \frac{1}{2} \left[\frac{27}{2} + \frac{9}{2} \right] = (18 - 9) \text{ sq. units} = 9 \text{ sq. units} \end{aligned}$$

66. (B)

$$y = \cos^{-1} \left(\frac{2\cos x - 3\sin x}{\sqrt{13}} \right) = \cos^{-1} (\cos \alpha \cos x - \sin \alpha \sin x)$$

$$\text{where } \sin \alpha = \frac{3}{\sqrt{13}}; \quad \cos \alpha = \frac{2}{\sqrt{13}} \quad \therefore \tan \alpha = \frac{3}{2}$$

$$= \cos^{-1} \cos(x + \alpha) = x + \alpha = x + \tan^{-1} \left(\frac{3}{2} \right)$$

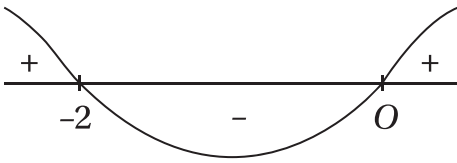
$$\therefore \frac{dy}{dx} = 1$$

67. (D)

$$y = x^2 e^x$$

$$\frac{dy}{dx} = 2xe^x + x^2 e^x = xe^x (2 + x)$$

Critical points: $x = 0, x = -2$



$$f'(x) < 0 \quad \forall x \in (-2, 0)$$

$$f'(x) > 0 \quad \forall x \in (-\infty, -2) \cup (0, \infty)$$

68. (B)

$$f(x) = \frac{1 - \cos \lambda x}{x \sin x}; \quad x \neq 0$$

$$= \frac{1}{2}; \quad x = 0$$

$$\therefore f(0) = \frac{1}{2}$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos \lambda x}{x \sin x} = \lim_{x \rightarrow 0} \frac{1 - \cos \lambda x}{(\lambda x)^2} \times \frac{\lambda^2 x}{\sin x} = \frac{1}{2} \times \lambda^2 = \frac{\lambda^2}{2}$$

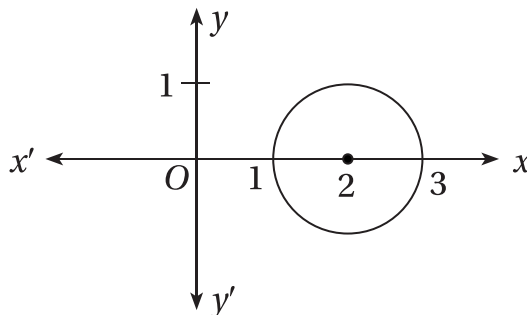
For continuous at $x = 0$,

$$\frac{\lambda^2}{2} = \frac{1}{2} \Rightarrow \lambda^2 = 1 \Rightarrow \lambda = \pm 1$$

69. (B)

$$y = \sqrt{(x-1)(3-x)} \Rightarrow y^2 = 3x - x^2 - 3 + x \Rightarrow x^2 + y^2 - 4x = -3 \Rightarrow (x-2)^2 + y^2 = 1$$

$$\therefore 0 \leq y \leq 1$$



70. ©

$$\begin{aligned}\cos^{-1}\left(-\sin\frac{7\pi}{6}\right) &= \cos^{-1}\left\{-\sin\left(\pi + \frac{\pi}{6}\right)\right\} = \cos^{-1}\left(\sin\frac{\pi}{6}\right) \\ &= \cos^{-1}\left\{\cos\left(\pi/2 - \pi/6\right)\right\} = \cos^{-1}\left\{\cos\frac{\pi}{3}\right\} = \frac{\pi}{3}\end{aligned}$$

71. ⑥

$$\begin{aligned}I &= \int_{\frac{\pi}{8}}^{\frac{7\pi}{8}} \frac{x dx}{\cos^2 x - \sin^2 x} = \int_{\frac{\pi}{8}}^{\frac{7\pi}{8}} \frac{(\pi - x) dx}{\cos 2(\pi - x)} = \pi \int_{\frac{\pi}{8}}^{\frac{7\pi}{8}} \frac{dx}{\cos 2x} - I \\ \Rightarrow 2I &= \pi \int_{\frac{\pi}{8}}^{\frac{7\pi}{8}} \sec 2x dx \\ \Rightarrow I &= \frac{\pi}{2} \times \frac{1}{2} \left[\log(\sec 2x + \tan 2x) \right]_{\frac{\pi}{8}}^{\frac{7\pi}{8}} = \frac{\pi}{4} \left[\log(\sqrt{2} - 1) - \log(\sqrt{2} + 1) \right] \\ &= \frac{\pi}{4} \log\left(\frac{\sqrt{2} - 1}{\sqrt{2} + 1}\right) = \frac{\pi}{4} \log(3 - 2\sqrt{2})\end{aligned}$$

72. ⑥

$$\begin{aligned}\int \frac{3^x dx}{\sqrt{1-9^x}} &= \frac{1}{\log_e 3} \int \frac{dt}{\sqrt{1-t^2}} \quad 3^x = t \Rightarrow 3^x \log_e 3 dx = dt \Rightarrow 3^x dx = \frac{1}{\log_e 3} dt \\ &= \frac{1}{\log_e 3} \left[\sin^{-1} t \right] + c = \frac{1}{\log_e 3} \left[\sin^{-1}(3^x) \right] + c\end{aligned}$$

73. ①

$$\int \tan^4 x dx = a \tan^3 x + b \tan x + cx$$

L.H.S

$$= \int \tan^2 x (\sec^2 x - 1) dx = \frac{\tan^3 x}{3} - \int (\sec^2 x - 1) dx = \frac{\tan^3 x}{3} - \tan x + x$$

$$\therefore a = \frac{1}{3}, \quad b = -1, \quad c = 1$$

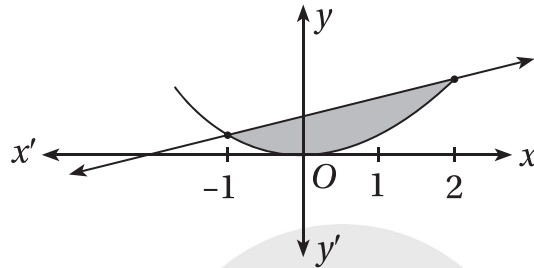
74. (B)

$$\int \left(\frac{1}{\log x} - \frac{1}{(\log x)^2} \right) dx = \int \frac{dx}{\log x} - \int \frac{dx}{(\log x)^2} = \frac{1}{\log x} \times x - \int -\frac{1}{(\log x)^2} \times \frac{1}{x} \times x dx - \int \frac{dx}{(\log x)^2}$$

$$= \frac{x}{\log x} + \int \frac{dx}{(\log x)^2} - \int \frac{dx}{(\log x)^2} = \frac{x}{\log x} + c$$

75. (B)

$$x^2 = 4y, \quad x = 4y - 2$$



$$x^2 = x + 2 \Rightarrow x^2 - x - 2 = 0 \Rightarrow (x - 2)(x + 1) = 0 \Rightarrow x = 2, -1$$

$$\therefore x = 2, y = 1$$

$$x = -1, y = \frac{1}{4}$$

$$\therefore \text{Area} = \int_{-1}^2 \frac{x+2}{4} dx - \int_{-1}^2 \frac{x^2}{4} dx = \frac{1}{4} \left[\frac{x^2}{2} + 2x \right]_{-1}^2 - \frac{1}{4} \left[\frac{x^3}{3} \right]_{-1}^2$$

$$= \frac{1}{4} \left[2 + 4 - \frac{1}{2} + 2 \right] - \frac{1}{12} [8 + 1] = \frac{1}{4} \times \frac{15}{2} - \frac{9}{12} = \frac{15}{8} - \frac{3}{4} = \frac{9}{8} \text{ sq. units}$$

Biology

76. (A)

Bone marrow

They make lymphocytes

77. (A)

IgA

78. (A)

It is used for cutting DNA at a specific location

It acts as a molecular scissor

79. Ⓐ
Salmonella typhimurium
80. Ⓐ
Amplification of gene of interest
81. Ⓒ
Biopiracy
82. Ⓑ
Insecticide
The toxin destroys the gut of the insects
83. Ⓓ
All
84. Ⓑ
The toxin is inactive in bacteria
It is toxic only to the insect pests
85. Ⓐ
Both A and R are true and R is the correct explanation of A
86. Ⓓ
A is false but R is true
Plasmids are extra chromosomal circular DNA
87. Ⓑ
Both A and R are true but R is not the correct explanation of A
88. Ⓑ
Malignant tumour
Cells from the original tumour break apart and move to other parts of the body
89. Ⓓ
All
90. Ⓒ
Immunotherapy
91. Ⓑ
2 celled stage
92. Ⓒ
Parturition

93. Ⓐ
Amniocentesis
It is a method of prenatal sex determination
94. Ⓓ
All of the above
95. Ⓑ
Convergent evolution
96. Ⓓ
Sporozoites
97. Ⓓ
E.coli cloning vector
98. Ⓐ
The sequence from where replication starts
Ori stands for origin
99. Ⓒ
Transformation
100. Ⓐ
Both A and R are true and R is the correct explanation of A.

