



# Monthly Progressive Test

Class: XI

Subject: PCMB

## Solution

### Physics

1. Ⓓ

like [velocity] =  $LT^{-1}$ , [Force] =  $MLT^{-2}$

2. Ⓐ

$$[z] = [x] \frac{L}{T^2}$$

and  $[x] = [y][w]$ , put dimensional formula of  $y$ , then we get dimensional formula of  $w$ .

3. Ⓐ

as  $(P - Q)$  is invalid

4. Ⓓ

force =  $2y \cdot \left(\frac{R}{x^2}\right)$ ; since  $\frac{10R}{x^2}$  is acceleration,  $2y$  is mass.

$$\text{Mass} = \frac{2y}{10} = \frac{y}{5} = \frac{10}{5} = 2\text{kg}$$

5. Ⓐ

as refractive index is dimensionless quantity

6. Ⓐ

equations of Kinematics are independent of mass

7. Ⓒ

$$\frac{h'}{h} = \frac{t^2}{100} \Rightarrow h' = \frac{h}{4}, h - h' = \frac{3h}{4} \text{ from ground}$$

8. (B)

$$v = \frac{dx}{dt} = -\left(\frac{4}{3}\right)^t + 16 = 0 \Rightarrow t = 12s$$

9. (B)

$$s = at + bt^2 \Rightarrow \frac{ds}{dt} = v = a + 2bt, \text{ again } a = \frac{dv}{dt} = 2b$$

10. (A)

$$\text{use average velocity} = \left[ \frac{(u+v)}{2} \right]$$

11. (D)

$$v = \alpha t_1 = \beta t_2 \Rightarrow t = t_1 + t_2 = \frac{v(\alpha + \beta)}{\alpha\beta} \Rightarrow v = \frac{\alpha\beta t}{\alpha + \beta}$$

12. (A)

magnitude of velocity remains same at same level

13. (D)

$s =$  area of graph

$$= \left(\frac{1}{2}\right) \times 2 \times 3 - \left(\frac{1}{2}\right)(1)(2) + (1)(1) = 3m$$

14. (A)

apply formula  $s = u + \frac{1}{2}a(2n-1)$  with  $u = 0$

$$\text{we get } \frac{10-1}{8-1} = \frac{9}{7}$$

15. (D)

as they fall down with same amount from top

16. (C)

alternate angle

17. (D)

$$s = \left[ \frac{(0+10)}{2} \right] \times 5 = 25m$$

18. (C)

$$s = \left(\frac{1}{2}\right)a.t^2 = \left(\frac{1}{2}\right)(3)(2)^2 = 6m \text{ as } u = 0 \text{ m/s}$$

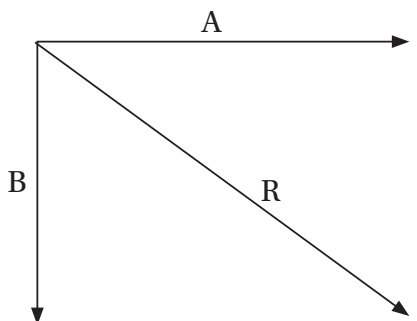
19. (B)

$$\text{average velocity} = \frac{2x}{\frac{x}{u} + \frac{x}{v}} = \frac{2uv}{u+v}$$

20. (A)

$$R^2 = P^2 + P^2 + 2P^2 \cos 120^\circ \Rightarrow R = P$$

21. (D)



22. (C)

$$|\hat{A}| = 1$$

23. (A)

$$\text{unit vector} = \frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{1+1+1}} = \frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$$

24. (B)

$$A - B = \hat{i} + \hat{j} - \hat{i} + \hat{j} = 2\hat{j} \quad |A - B| = 2 \text{ unit}$$

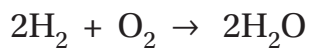
25. (A)

$$V_{wg} = 4\hat{i} \text{ m/s}; V_{rw} = -3\hat{j} \text{ m/s}$$

$$\text{Apply, } V_{rw} = V_{rg} - V_{wg}$$

## Chemistry

26. (D)



$$4\text{g} \quad 32\text{g} \quad 2 \times 18 = 36\text{g}$$

$$\text{Given } 10\text{g} \quad 64\text{g} \quad ?$$

(L.R)

$$32\text{g O}_2 \equiv 36\text{g H}_2\text{O}$$

$$\begin{aligned}
 64\text{g O}_2 &\equiv \frac{36 \times 64}{32} \text{g H}_2\text{O} \\
 &\equiv 72\text{g H}_2\text{O} \\
 &\equiv \frac{72}{18} \text{g moles water} \\
 &\equiv 4 \text{ moles water}
 \end{aligned}$$

27. ③



∴ 1 mole magnesium phosphate = 8 moles of oxygen atom.

∴ 8 moles oxygen atom = 1 mole magnesium phosphate

$$\begin{aligned}
 0.25 \text{ moles oxygen atom} &= \frac{1 \times 0.25}{8} = 0.03125 \text{ mole magnesium phosphate} \\
 &= 3.125 \times 10^{-2} \text{ mole magnesium phosphate}
 \end{aligned}$$

28. ③



$$5(12+16)\text{g} \qquad \qquad \qquad 2 \times 127 = 254\text{g}$$

$$= 140\text{g}$$

$$\therefore 254\text{g I}_2 = 140\text{g CO}$$

$$2.54\text{g I}_2 = \frac{140 \times 2.54}{254} \text{g} = 1.40\text{g}$$

$$\therefore \text{Mass of CO}_2 = 2 - 1.40 = 0.6\text{g}$$

$$\therefore \text{Mass \% of CO}_2 = \frac{0.6}{2\text{g}} \times 100\% = 30\%$$

29. ③

Element	%	At. Wt.	R.A.M	Simplest Ratio
C	10.06	12	$\frac{10.06}{12} = 0.83$	$\frac{0.83}{0.83} = 1$
H	0.84	1	$\frac{0.84}{1} = 0.84$	$\frac{.84}{.83} = 1.01 \approx 1$
Cl	89.10	35.5	$\frac{89.10}{35.5} = 2.5$	$\frac{2.5}{0.83} = 3$

[5]

∴ Empirical formula =  $\text{CHCl}_3$

30. Ⓑ

In oxides sulphur

S = 50% ∴ oxygen (O) = 100 - 50 = 50%

Element	%	At. Wt.	R.A.M	Simplest Ratio
S	50	32	$\frac{50}{32} = 1.56$	$\frac{1.56}{1.56} = 1$
O	50	16	$\frac{50}{16} = 3.12$	$\frac{3.125}{1.56} = 2$

∴ Empirical formula =  $\text{SO}_2$

31. Ⓓ

$$8\text{gO}_2 = \frac{8}{32} \text{ moles} = \frac{1}{4} \times \text{No molecules}$$

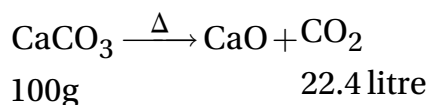
$$7\text{gCO} = \frac{7}{28} \text{ moles} = \frac{1}{4} \times \text{No molecules}$$

$$11\text{gCO}_2 = \frac{11}{44} \text{ mole} = \frac{1}{4} \times \text{No molecules}$$

$$7\text{g of N}_2 = \frac{7}{28} \text{ moles} = \frac{1}{4} \times \text{No molecules (No = Avogadro number)}$$

32. Ⓓ

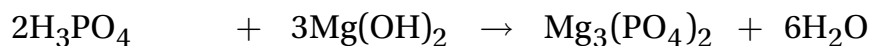
$$90\% \text{ of } 10\text{g} = \frac{90}{100} \times 10\text{g} = 9\text{g pure CaCO}_3$$



∴ 100g  $\text{CaCO}_3$  = 22.4 lt.  $\text{CO}_2$  at S.T.P

$$\therefore 9\text{g} \quad ,, \quad = \frac{22.4 \times 9}{100} \text{ L CO}_2 = 2.016 \text{ L CO}_2$$

33. Ⓑ



$$2(3+31+64) \quad 3(24+2 \times 17)$$

$$= 2 \times 98\text{g} \quad = 3 \times 58\text{g}$$

$$\therefore 3 \times 58\text{g Mg(OH)}_2 = 2 \times 98\text{g H}_3\text{PO}_4$$

[6]

$$\begin{aligned}\therefore 100\text{g Mg(OH)}_2 &= \frac{2 \times 98 \times 100}{3 \times 58} \text{gH}_3\text{O}_4 \\ &= 112.64\text{g H}_3\text{PO}_4 \\ \therefore 112\text{g H}_3\text{PO}_4\end{aligned}$$

34. Ⓑ

Molarity depends on temperature as it depends on volume.

Mole fraction, Molarity do not change with temperature as they depend on mass.

35. Ⓐ

At S.T.P. = 22.4L N<sub>2</sub> = 6.023 × 10<sup>23</sup> molecules N<sub>2</sub>

$$1.12\text{L N}_2 = \frac{6.023 \times 10^{23} \times 1.12}{22.4} \text{ molecules N}_2 = 3.01 \times 10^{22}$$

36. Ⓒ

$$\text{ZnO} = 65 + 16 = 81; \% \text{ of O} = \frac{16}{81} \times 100\% = 19.7\%$$

$$\text{Na}_2\text{O} = 46 + 16 = 62; \% \text{ of O} = \frac{16}{82} \times 100 = 25.8$$

$$\text{MgO} = 24 + 16 = 40; \% \text{ of O} = \frac{16}{40} \times 100 = 40\%$$

$$\text{N}_2\text{O} = 28 + 16 = 44; \% \text{ of O} = \frac{16}{44} \times 100 = 36\%$$

37. Ⓑ

$$\text{H}_2\text{SO}_4 = 2 + 32 + 4 \times 16 = 98$$

$$\% \text{ of 'O'} = \frac{64}{98} \times 100 = 65.3\%$$

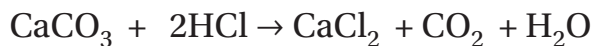
38. Ⓓ

$$V_1M_1 + V_2M_2 = (V_1 + V_2) M_3$$

$$\text{or } 200 \times 1 + 300 \times 0.2 = 500 \times x$$

$$\text{or } x = 0.52$$

39. Ⓑ



$$100 \quad 2 \times 36$$

Given : 40g      25g (L.R)

$$100\text{gCaCO}_3 = 2 \times 36\text{g HCl}$$

[7]

$$40\text{g CaCO}_3 = \frac{2 \times 36 \times 40}{100} \text{ of HCl}$$

$$= 28.8\text{g HCl (Need)}$$

But given 25g. So, HCl is Limiting Regret.

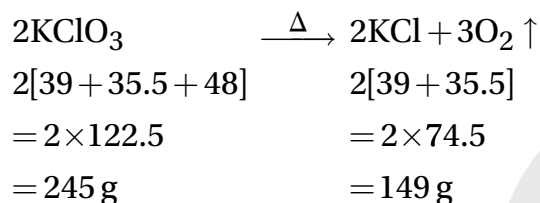
Again,  $2 \times 36\text{g HCl} = 100\text{g CaCO}_3$

$$25\text{g HCl} = \frac{100 \times 25}{2 \times 36} \text{ of CaCO}_3$$

$$= 34.72\text{g CaCO}_3 \text{ (Need)}$$

But,  $\text{CaCO}_3$  Present 40g. So,  $\text{CaCO}_3$  is in excess

40. (B)



$245\text{g KClO}_3 = 149\text{g KCl}$ $\therefore 1.22\text{g} = \frac{149 \times 1.22}{245}$ $= 0.74\text{g}$	$245\text{g KClO}_3 = 3 \times 22.4\text{LO}_2$ $1.22\text{g} = \frac{3 \times 22.4}{245} \times 1.22$ $= 0.335\text{LO}_2$
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41. (C)

28g  $\text{N}_2$  produces  $(2 \times 17)\text{g}$  of  $\text{NH}_3$

$$\therefore 5.6\text{g N}_2 \text{ produces } \frac{2 \times 17 \times 5.6}{28} = 6.8\text{g of NH}_3$$

42. (B)

Molecular weight of  $\text{CaCO}_3 = 40 + 12 + 48 = 100$

100g  $\text{CaCO}_3 = 6.02 \times 10^{23}$   $\text{CaCO}_3$  molecule

$$1\text{g} \quad ,, \quad = \left[ \frac{6.02 \times 10^{23}}{100} \right] = 6.02 \times 10^{21} \text{ molecules}$$

43. (C)

One  $\text{CaCO}_3$  molecule contains 5 atoms and molecular weight of  $\text{CaCO}_3 = 40 + 12 + 48 = 100$

100g  $\text{CaCO}_3$  contain  $(5 \times 6.02 \times 10^{23})$  atoms

$$20\text{g CaCO}_3 \text{ contain } \left( \frac{5 \times 6.02 \times 10^{23}}{100} \times 20 \right) \text{ atom}$$

$$= 6.02 \times 10^{23} \text{ atom}$$

44. Ⓓ

$$\text{For oxygen} = \frac{3.01 \times 10^{22}}{6.02 \times 10^{23}} = \frac{1}{20} = 0.05 \text{ moles}$$

$$\text{For hydrogen} = \frac{560}{22400} = \frac{1}{20} = 0.025 \text{ moles}$$

$$\text{So, total number of moles} = (0.05 + 0.025) = 0.075 \text{ moles}$$

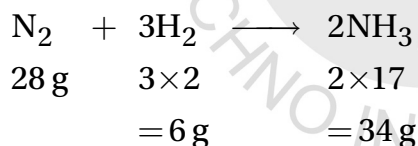
45. Ⓑ

$$0.355 \text{ g Cl}_2 = \frac{0.355}{71} = 0.005 \text{ mole Cl}_2$$

$$1.204 \times 10^{23} \text{ O}_2 \text{ molecules} = \frac{1.204 \times 10^{23}}{6.02 \times 10^{23}} = 0.2 \text{ mole of O}_2$$

$$0.112 \text{ L N}_2 \text{ at STP} = \frac{0.112}{22.4} = 0.005 \text{ mole N}_2$$

46. Ⓐ



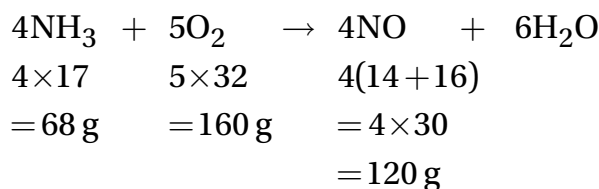
$$\text{Given : } 2\text{g} \quad 2\text{g}$$

(L.R)

$6\text{gH}_2 = 28\text{g N}_2$ So, $2\text{gH}_2 = \frac{28 \times 2}{6} \text{g N}_2$ $= 9.33\text{g N}_2 \text{ (required) L.R.}$	$28\text{g N}_2 = 6\text{g H}_2$ $\therefore 2\text{g N}_2 = \frac{6 \times 2}{28} \text{g H}_2$ $= 0.42\text{g H}_2 \text{ (Need)}$
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So, H<sub>2</sub> is excess

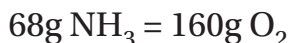
47. Ⓓ





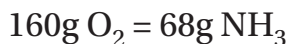
Given : 1.7g            4g

(L.R)



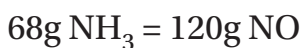
$$\text{So, } 1.7\text{g NH}_3 = \frac{160 \times 1.7}{68} \text{g O}_2$$

$$= 4\text{g O}_2 \text{ (Need)}$$



$$\therefore 4\text{g O}_2 = \frac{68 \times 4}{160} \text{g NH}_3 = 1.7\text{g NH}_3 \text{ (Need)}$$

So, NH<sub>3</sub> is the limiting reagent



$$1.7\text{g NH}_3 = \frac{120 \times 1.7}{68} \text{g NO} = 3\text{g NO}$$

48. (B)

$$200 \text{ ml } 0.2 \text{ (N) NaOH} = (2.00 - 25) \times x \text{ (N)}$$

$$\Rightarrow x = \frac{200 \times 0.2}{175} \text{ (N)}$$

$$\Rightarrow x = 0.22\text{g}$$

49. (A)

$$\begin{aligned} \text{Molarity (M')} &= \frac{w \times 6000}{m \times V(\text{c.c})} \\ &= \frac{0.3 \times 1000}{60 \times 500} = 0.01 \text{ (M)} \end{aligned}$$

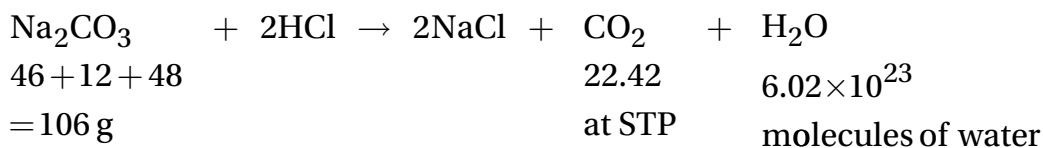
Let, the final concentration be x ; (n factor of urea =1)

Acc problem,

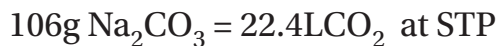
$$500 \times 0.01 = 1250x$$

$$\Rightarrow x = \frac{500 \times 0.01}{1250} = 0.004 \text{ (M)}$$

50. (C)



Given : 0.53g



$$0.53\text{ g Na}_2\text{CO}_3 = \frac{22.4 \times 0.53}{106}\text{L} = 0.112\text{L CO}_2$$

Again,  $106\text{g Na}_2\text{CO}_3 = 6.023 \times 10^{23}$  molecules  $\text{H}_2\text{O}$

$$\begin{aligned} 0.53\text{ g Na}_2\text{CO}_3 &= \frac{6.023 \times 10^{23}}{106} \times 0.53 \\ &= 0.0301 \times 10^{23} \text{ molecule of H}_2\text{O} \\ &= 3.01 \times 10^{21} \text{ molecule of H}_2\text{O} \end{aligned}$$

## Mathematics

51. ©

$$\text{Given } \frac{x}{\cos\theta} = \frac{y}{\cos\left(\theta + \frac{2\pi}{3}\right)} = \frac{z}{\cos\left(\theta - \frac{2\pi}{3}\right)} = \lambda \text{ (say)}$$

$$\Rightarrow x + y + z = \lambda \left\{ \cos\theta + \cos\left(\theta + \frac{2\pi}{3}\right) + \cos\left(\theta - \frac{2\pi}{3}\right) \right\} = \lambda \left\{ \cos\theta + 2\cos\theta \cos\frac{2\pi}{3} \right\} = 0$$

52. ©

$$\text{Given } \sin\theta_1 + \sin\theta_2 + \sin\theta_3 = 3 \Rightarrow \sin\theta_1 = \sin\theta_2 = \sin\theta_3 = 1$$

( $\because$  maximum value of  $\sin x$  is 1, therefore, given statement is possible only when each term on L.H.S. is equal to 1)

$$\Rightarrow \cos\theta_1 = \cos\theta_2 = \cos\theta_3 = 0 \quad (\because \cos^2 x = 1 - \sin^2 x \forall x)$$

$$\Rightarrow \cos\theta_1 = \cos\theta_2 = \cos\theta_3 = 0$$

53. ©

$$\text{Let } \sin A + \sin B = a \quad \dots (1)$$

$$\text{and } \cos A + \cos B = b \quad \dots (2)$$

$$\cos 2A + \cos 2B + 2\cos(A+B) = b^2 - a^2.$$

$$\text{So, } 2\cos(A+B)\cos(A-B) + 2\cos(A+B) = b^2 - a^2.$$

$$\text{or } \cos(A+B)\{2\cos(A-B) + 2\} = b^2 - a^2 \quad \dots (3)$$

$$2 + 2\cos(A-B) = \frac{b^2 - a^2}{\cos(A+B)} \quad \dots \text{ [Use this in (3)]}$$

$$\cos(A+B)(a^2 + b^2) = (b^2 - a^2).$$

$$\text{or } \cos(A+B) = \frac{(b^2 - a^2)}{(a^2 + b^2)}$$

54. Ⓑ

$$\begin{aligned}
& 3 \left[ \sin^4 \left( \frac{3\pi}{2} - \alpha \right) + \sin^4 (3\pi + \alpha) \right] - 2 \left[ \sin^6 \left( \frac{\pi}{2} + \alpha \right) + \sin^6 (5\pi - \alpha) \right] \\
&= 3[\cos^4 \alpha + \sin^4 \alpha] - 2[\cos^6 \alpha + \sin^6 \alpha] \\
&= 3 \left[ (\cos^2 \alpha + \sin^2 \alpha)^2 - 2\cos^2 \alpha \sin^2 \alpha \right] \\
&\quad - 2 \left[ (\cos^2 \alpha + \sin^2 \alpha)^3 - 3\cos^2 \alpha \sin^2 \alpha (\cos^2 \alpha + \sin^2 \alpha) \right] \\
&= 3[1 - 2\cos^2 \alpha \sin^2 \alpha] - 2[1 - 3\cos^2 \alpha \sin^2 \alpha] \\
&= 3 - 6\cancel{\cos^2 \alpha \sin^2 \alpha} - 2 + 6\cancel{\cos^2 \alpha \sin^2 \alpha} \\
&= 1
\end{aligned}$$

55. Ⓒ

$$\begin{aligned}
& 3(\sin x - \cos x)^4 + 6(\sin x + \cos x)^2 + 4(\sin^6 x + \cos^6 x) \\
&= 3(1 - 2\sin x \cos x)^2 + 6(1 + 2\sin x \cos x) + 4[1 - 3\sin^2 x \cos^2 x] \\
&= 3(1 - 4\sin x \cos x + 4\sin^2 x \cos^2 x) + 6 + 12\sin x \cos x + 4 - 12\sin^2 x \cos^2 x \\
&= 3 - 12\cancel{\sin x \cos x} + 12\cancel{\sin^2 x \cos^2 x} + 6 + 12\cancel{\sin x \cos x} + 4 - 12\cancel{\sin^2 x \cos^2 x} \\
&= 13
\end{aligned}$$

56. Ⓒ

$$\begin{aligned}
A - B = \frac{\pi}{4} &\Rightarrow \tan(A - B) = \tan \frac{\pi}{4} \\
&\Rightarrow \frac{\tan A - \tan B}{1 + \tan A \tan B} \\
&\Rightarrow \tan A - \tan B - \tan A \tan B = 1 \\
&\Rightarrow \tan A - \tan B - \tan A \tan B + 1 = 2 \\
&\Rightarrow (1 + \tan A)(1 - \tan B) = 2 \Rightarrow y = 2 \\
\text{Hence, } (y + 1)^{y+1} &= (2 + 1)^{2+1} = (3)^3 = 27
\end{aligned}$$

57. Ⓒ

$$\begin{aligned}
& \text{We have } \sin x + \sin^2 x = 1 \\
&\Rightarrow \sin x = 1 - \sin^2 x \Rightarrow \sin x = \cos^2 x
\end{aligned}$$

$$\begin{aligned} \text{Now } \cos^{12} x + 3 \cos^{10} x + 3 \cos^8 x + \cos^6 x - 2 &= \sin^6 x + 3 \sin^5 x + 3 \sin^4 x + \sin^3 x - 2 \\ &= (\sin^2 x)^3 + 3(\sin^2 x)^2 \sin x + 3(\sin^2 x)(\sin x)^2 + (\sin x)^3 - 2 = (\sin^2 x + \sin x)^3 - 2 \\ &= (1)^3 - 2 = -1 \end{aligned}$$

58. ©

$$\begin{aligned} \sin^2 \frac{\pi}{6} + \cos^2 \frac{\pi}{4} - \sec \frac{\pi}{3} \\ = \left(\frac{1}{2}\right)^2 + \frac{1}{2} - 2 = \frac{1}{4} + \frac{1}{2} - 2 = \frac{1+2-8}{4} = \frac{-5}{4} \end{aligned}$$

59. Ⓑ

$$\begin{aligned} \frac{1}{\sec \alpha - \tan \alpha} + \frac{1}{\sec \alpha + \tan \alpha} \\ = \frac{\sec \alpha + \tan \alpha + \sec \alpha - \tan \alpha}{\sec^2 \alpha - \tan^2 \alpha} = 2 \sec \alpha \end{aligned}$$

60. Ⓐ

$$\begin{aligned} (a \cos \theta + b \sin \theta)^2 + (a \sin \theta - b \cos \theta)^2 &= 9 + 16 \\ \Rightarrow a^2 + b^2 &= 25 \end{aligned}$$

61. ©

$$\begin{aligned} \operatorname{cosec} A + \cot A &= \frac{11}{2} \\ \Rightarrow \operatorname{cosec} A - \cot A &= \frac{2}{11} \\ \therefore 2 \cot A &= \frac{11}{2} - \frac{2}{11} = \frac{121-4}{22} = \frac{117}{22} \\ \cot A &= \frac{117}{44} \Rightarrow \tan A = \frac{44}{117} \end{aligned}$$

62. Ⓑ

$$\begin{aligned} \tan \alpha + \cot \alpha &= a \\ \Rightarrow \tan^2 \alpha + \cot^2 \alpha &= a^2 - 2 \\ \Rightarrow \tan^4 \alpha + \cot^4 \alpha + 2 &= a^4 - 4a^2 + 4 \\ \Rightarrow \tan^4 \alpha + \cot^4 \alpha &= a^4 - 4a^2 + 2 \end{aligned}$$

63. Ⓓ

$$\cos A = -\frac{5}{13} \text{ and } A \text{ is not in 3rd quadrant.}$$

$\therefore A$  is in 2nd quadrant.

$$\therefore \sin A = \frac{12}{13}, \quad \tan A = -\frac{12}{5}$$

$$\therefore \sin A - \tan A = \frac{12}{13} + \frac{12}{5} = \frac{60 + 156}{65} = \frac{216}{65}$$

64. (A)

$$\begin{aligned} & \cos(540^\circ - \theta) - \sin(630^\circ - \theta) \\ &= \cos(3 \times 180^\circ - \theta) - \sin(7 \times 90^\circ - \theta) \\ &= -\cos \theta + \cos \theta = 0 \end{aligned}$$

65. (D)

$$\begin{aligned} & \frac{\sin 13^\circ \cos 47^\circ + \cos 13^\circ \sin 47^\circ}{\cos 72^\circ \cos 12^\circ + \sin 72^\circ \sin 12^\circ} \\ &= \frac{\sin(13^\circ + 47^\circ)}{\cos(72^\circ - 12^\circ)} = \frac{\sin 60^\circ}{\cos 60^\circ} = \tan 60^\circ = \sqrt{3} \end{aligned}$$

66. (B)

$$\begin{aligned} \alpha + \beta &= K + 6, \quad \alpha\beta = 2(2K - 1) \\ \alpha + \beta &= \frac{1}{2} \alpha\beta \\ \Rightarrow K + 6 &= 2K - 1 \\ \Rightarrow K &= 7 \end{aligned}$$

67. (A)

$$\begin{aligned} \text{One root} &= 3 + 2\sqrt{3} \\ \therefore \text{other root} &= 3 - 2\sqrt{3} \\ \therefore \text{The quadratic equation is } &x^2 - 6x - 3 = 0 \end{aligned}$$

68. (B)

$$\begin{aligned} n(A \times B) &= n(A) \times n(B) \\ \Rightarrow 45 &= n(A) \times n(B) \\ \therefore n(A) &\text{ cannot be } 17 \end{aligned}$$

69. (C)

$$R: A \rightarrow B \quad \therefore R \subseteq A \times B$$

70. (C)

$$f(x) = x^3 - \frac{1}{x^3}$$

$$f\left(\frac{1}{x}\right) = \frac{1}{x^3} - x^3$$

$$\therefore f(x) + f\left(\frac{1}{x}\right) = 0$$

71. (B)

$$\begin{aligned} &= \frac{1}{\sin 1^\circ} [(\tan 1^\circ - \tan 0^\circ) + (\tan 2^\circ - \tan 1^\circ) + (\tan 3^\circ - \tan 2^\circ) + (\tan 4^\circ - \tan 3^\circ) \\ &\quad + \dots + (\tan 45^\circ - \tan 44^\circ)] \\ &= \frac{1}{\sin 1^\circ} = \frac{1}{x} \end{aligned}$$

72. (C)

$$5 \tan \theta = 4 \Rightarrow \tan \theta = \frac{4}{5}$$

$$\text{Now, } \frac{5 \sin \theta - 3 \cos \theta}{5 \sin \theta + 2 \cos \theta} = \frac{5 \frac{\sin \theta}{\cos \theta} - 3}{5 \frac{\sin \theta}{\cos \theta} + 2} = \frac{5 \tan \theta - 3}{5 \tan \theta + 2} = \frac{5 \times \frac{4}{5} - 3}{5 \times \frac{4}{5} + 2} = \frac{1}{6}$$

73. (B)

$$\begin{aligned} \frac{\sin(x+y)}{\sin(x-y)} &= \frac{a+b}{a-b} \\ \Rightarrow \frac{\sin(x+y) + \sin(x-y)}{\sin(x+y) - \sin(x-y)} &= \frac{(a+b) + (a-b)}{(a+b) - (a-b)} \\ \Rightarrow \frac{2 \sin x \cos y}{2 \cos x \sin y} &= \frac{2a}{2b} \\ \Rightarrow \frac{\tan x}{\tan y} &= \frac{a}{b} \end{aligned}$$

74. (D)

From the given relations,  $m + n = 2 \tan \theta$ ,  $m - n = 2 \sin \theta$

$$\Rightarrow m^2 - n^2 = 4 \tan \theta \sin \theta$$

$$\text{Also } 4\sqrt{mn} = 4\sqrt{\tan^2 \theta - \sin^2 \theta} = 4 \sin \theta \tan \theta$$

$$\therefore \text{From equations (i) and (ii), we get } m^2 - n^2 = 4\sqrt{mn}$$

75. (A)

$$\sin x + \operatorname{cosec} x = 2$$

$$\Rightarrow (\sin x - 1)^2 = 0 \Rightarrow \sin x = 1 \Rightarrow \sin^n x + \operatorname{cosec}^n x = 1 + 1 = 2$$

**Biology**

76. ©  
Metatheria
77. Ⓑ  
Tiny pebbles eaten by some birds are used in crushing  
Makes up for the lack of teeth
78. Ⓑ  
Ophiology
79. Ⓑ  
*Balanoglossus*
80. Ⓓ  
Whale-Ammonotelic
81. Ⓐ  
*Archaeopteryx*
82. Ⓓ  
Bat
83. Ⓓ  
Subphylum *Urochordata*
84. ©  
Ingestion
85. Ⓐ  
Male *Hippocampus*
86. Ⓑ  
Paedogenesis
87. Ⓓ  
Birds  
To meet the high demand for oxygen during flight
88. Ⓑ  
Nutrition
89. Ⓐ  
Incisors



90. Ⓓ  
Retina of owls contain only rods  
Bats have no cones in their retina as they are nocturnal.  
Rods are concerned with dim light or night vision
91. Ⓐ  
*Gingko*  
It continues to live with its ancient features that have shown no change over millions of years
92. Ⓐ  
Pteridophytes  
Only cryptogams to have xylem and phloem for transport of substances
93. Ⓒ  
Generic name and specific epithet
94. Ⓒ  
Basidiomycetes
95. Ⓒ  
Echinoderms
96. Ⓒ  
They are all tetrapods  
Have two pairs of limbs (modified as per the habitat)
97. Ⓓ  
To make the body light  
Adaptive feature to facilitate flight
98. Ⓓ  
Dry and cornified skin
99. Ⓓ  
III & IV
100. Ⓑ  
A-Post anal tail; B-Notochord; C- Dorsal nerve chord; D - Pharyngeal gill slits  
Basic features of embryos of all chordates